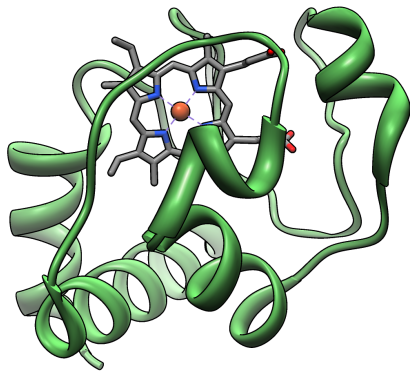


Neutral evolution and the acceleration of the molecular clock

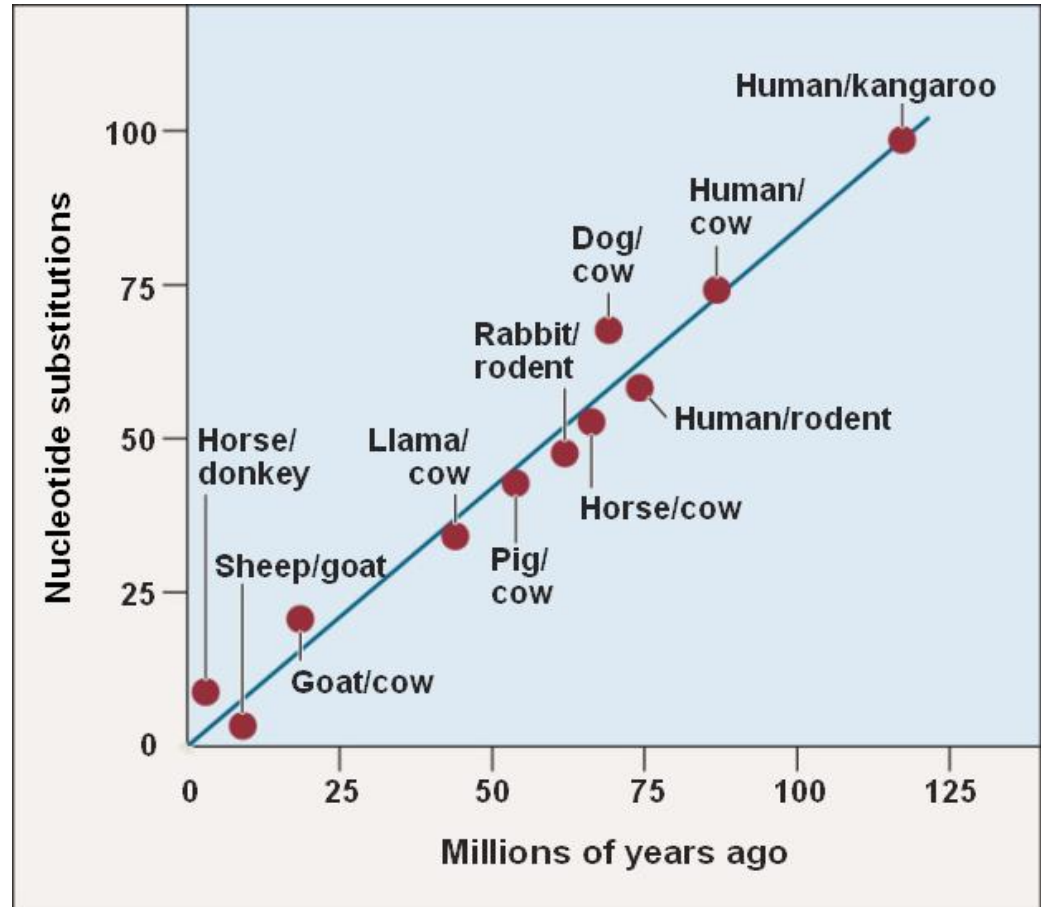


José A. Cuesta & Susanna Manrubia
Grupo Interdisciplinar de Sistemas Complejos
math UC3M & CNB-CSIC

empirical evidence of a molecular clock

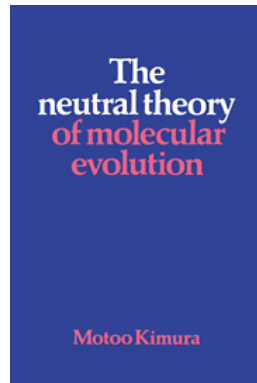


cytochrome c gene



Zuckerlandl & Pauling, *J. Theor. Biol.* (1965)

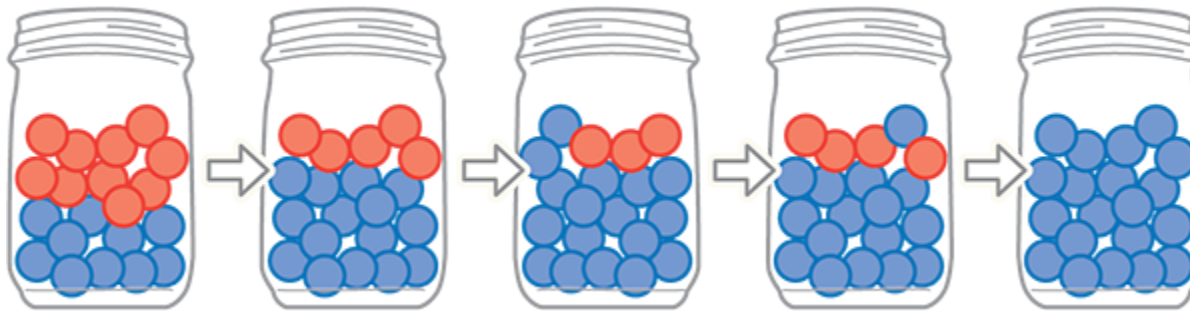
neutralist explanation



(1983)

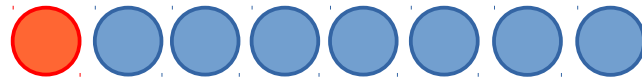


Motoo Kimura
(1924-1994)

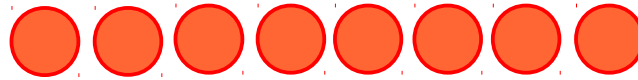


genetic drift

neutralist explanation



$$\pi_1 = \frac{1}{N}$$



population size



μN mutants/generation \times $1/N$ = μ mutations/generation go to fixation

neutral mutation rate

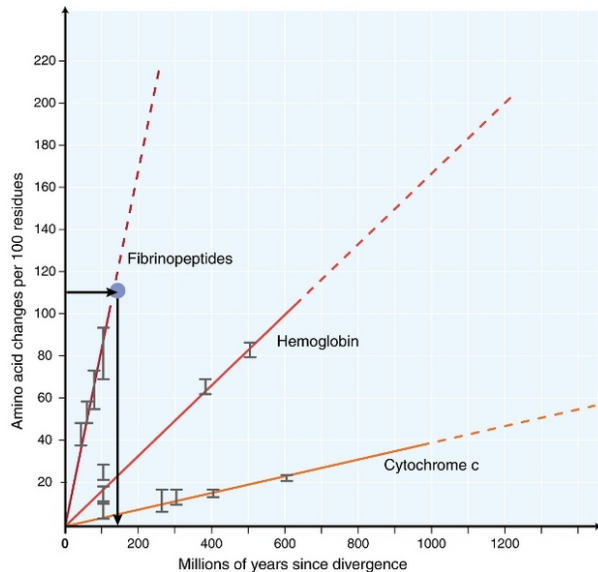


fixation probability

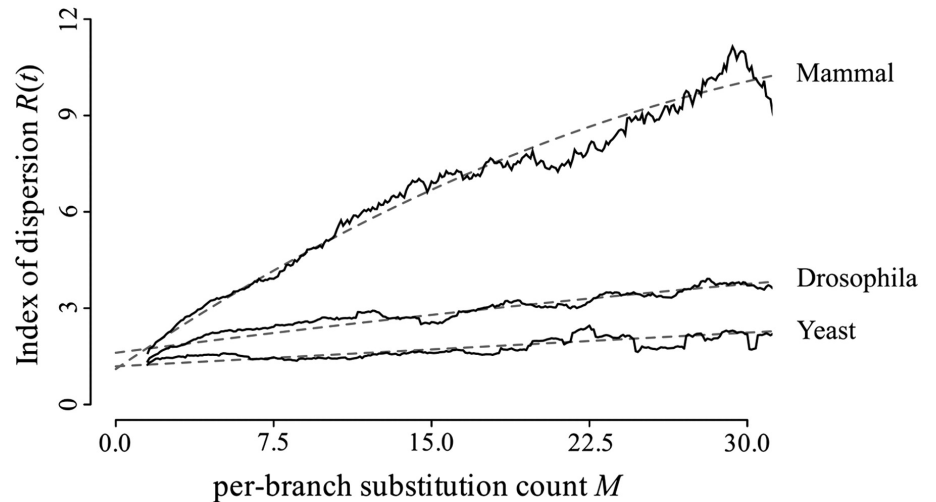


irregularities of the molecular clock

rate differences across lineages



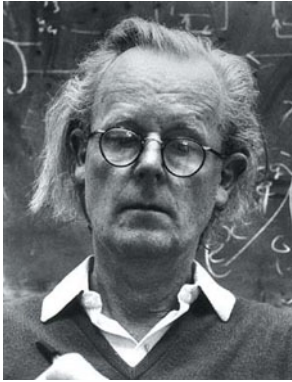
overdispersion



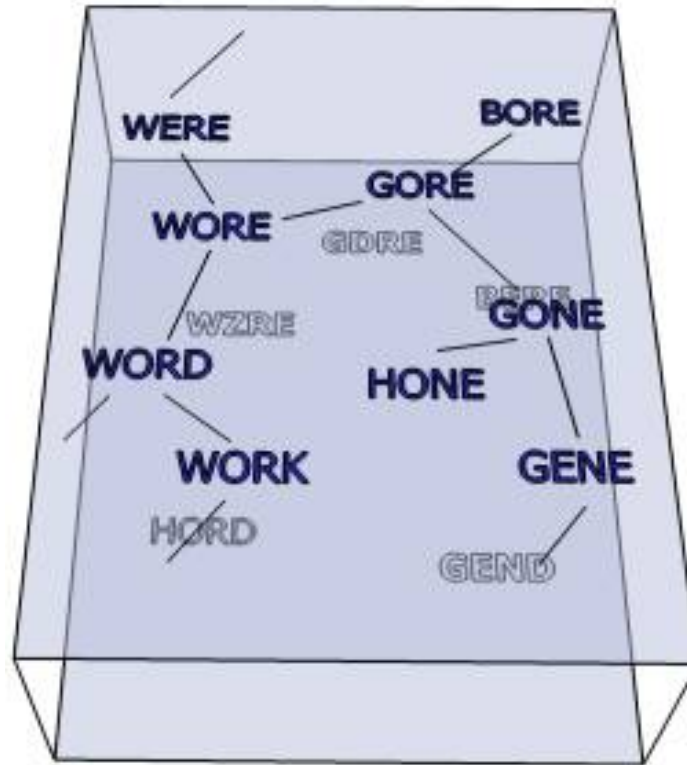
$$R(t) = \frac{\sigma^2}{\mu} = 1$$

Poisson process

neutral networks



John Maynard Smith
(1920-2004)



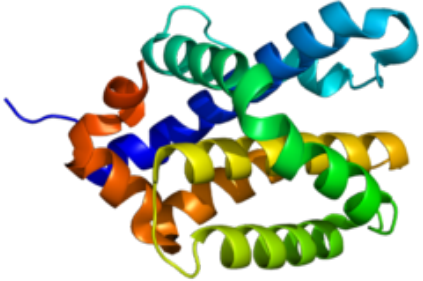
Maynard Smith, "Natural selection and the concept of a protein space", *Nature* (1970)

redundancy

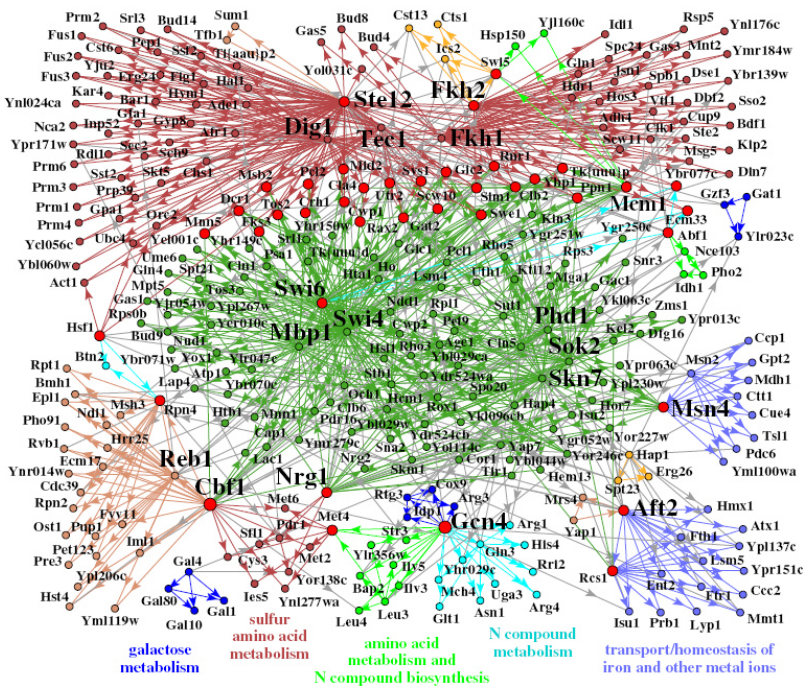
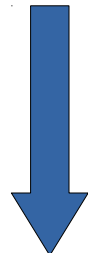


A
T
C
G

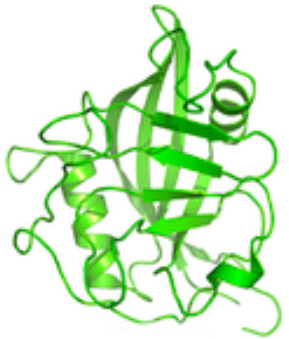
synonymous mutations



irrelevant structural changes



gene knock-out

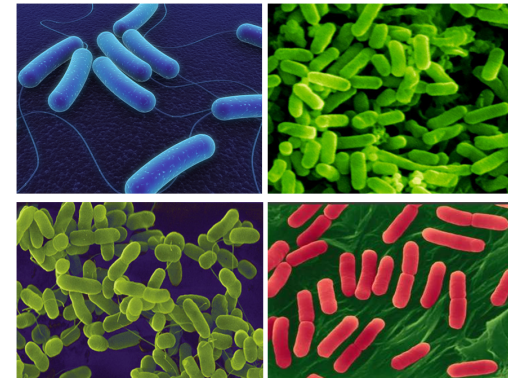
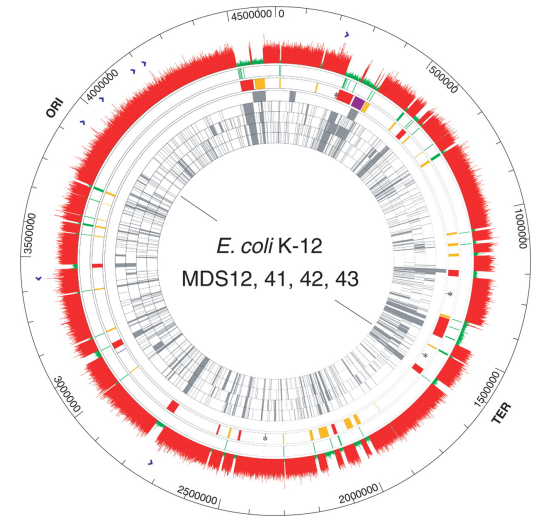
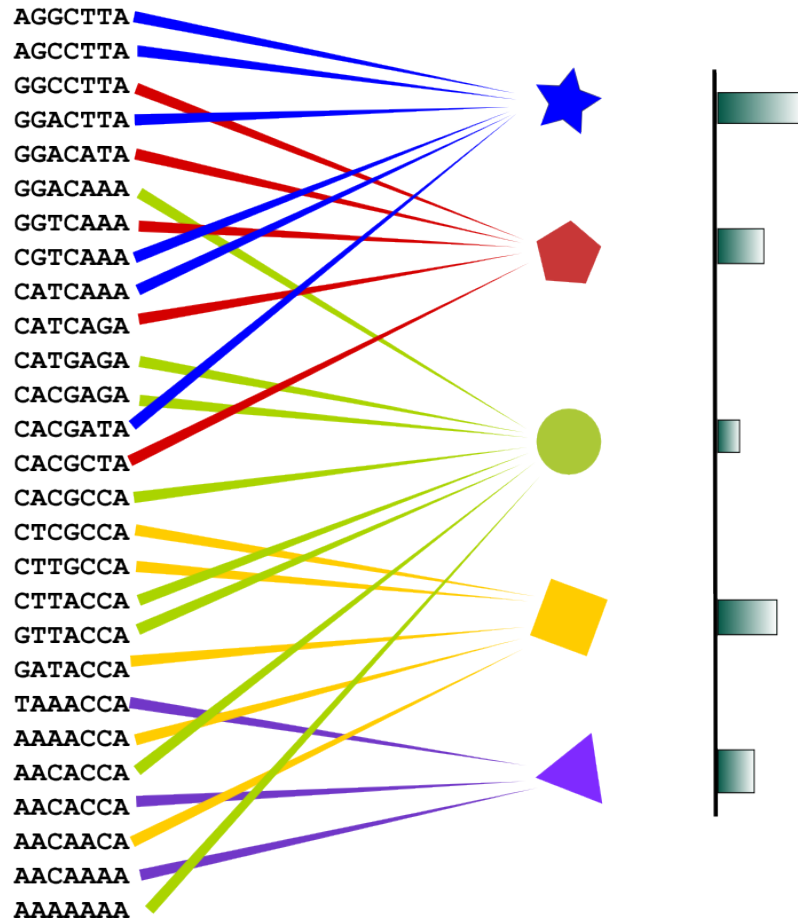


genotype-phenotype mapping

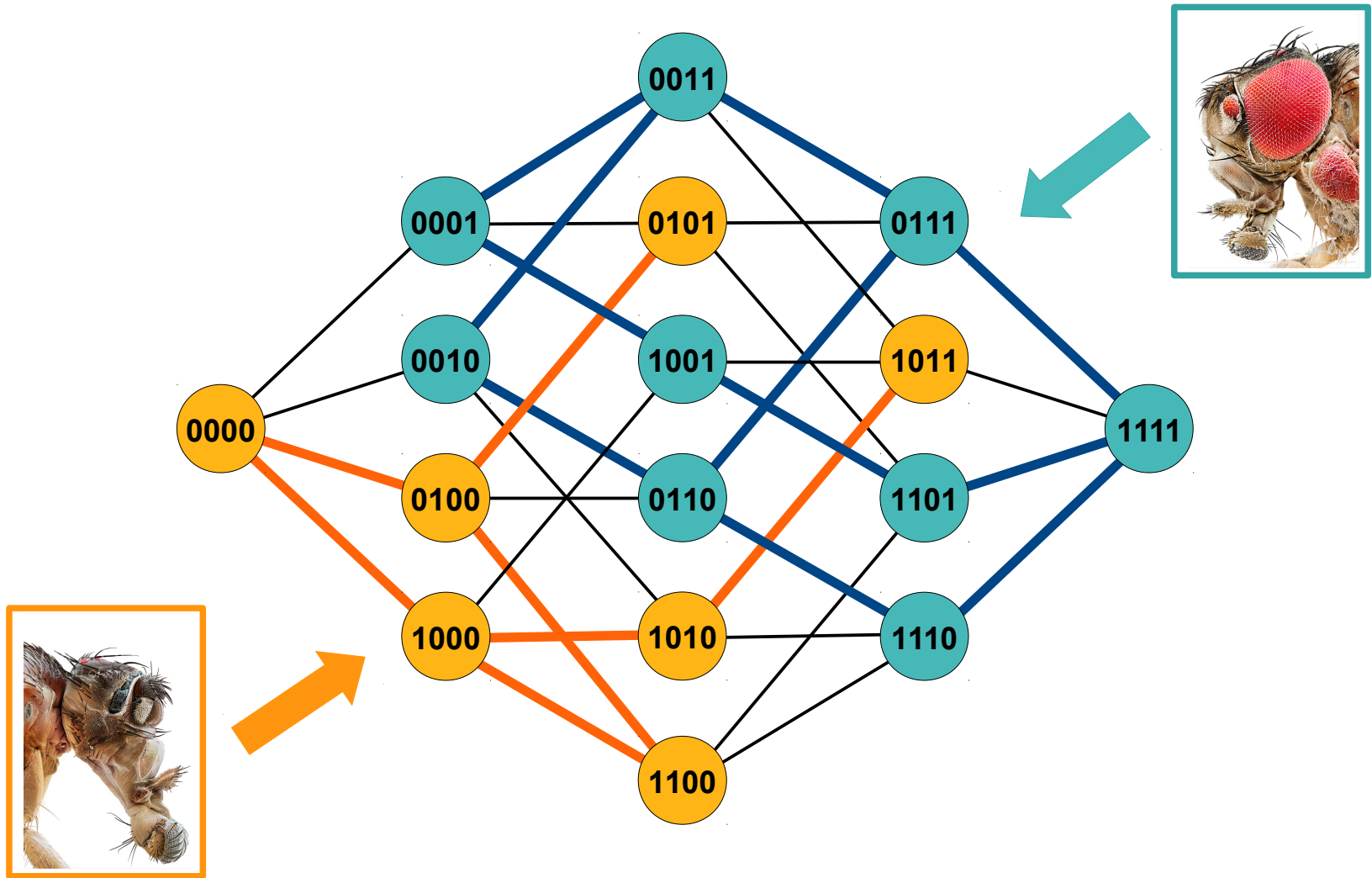
genotype

phenotype

fitness

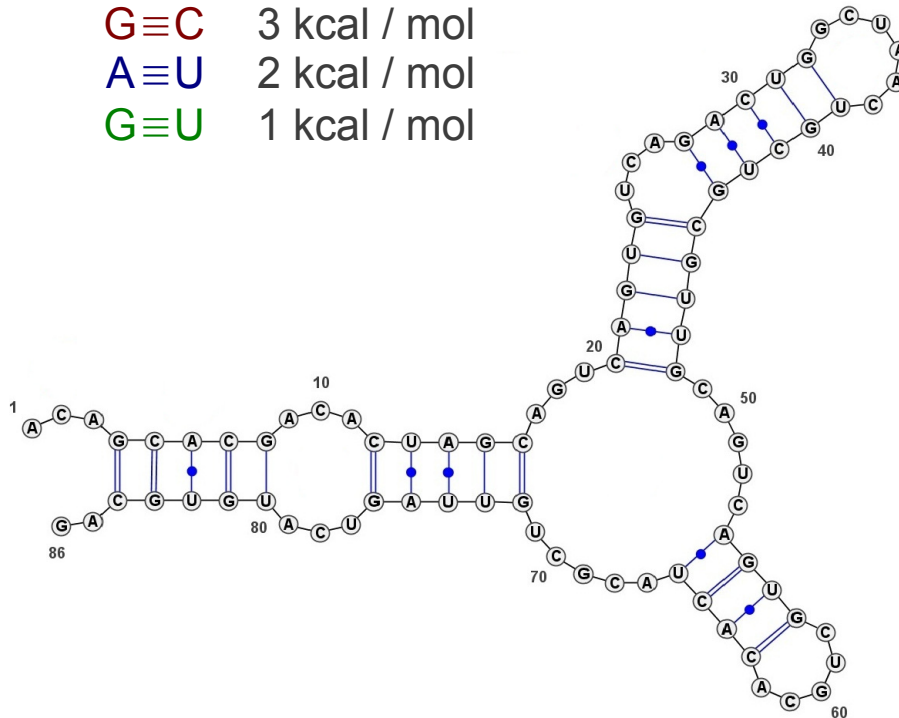


genotype networks



RNA secondary structure

G ≡ C 3 kcal / mol
A ≡ U 2 kcal / mol
G ≡ U 1 kcal / mol



mean number of sequences of length n folding into the same secondary structure:

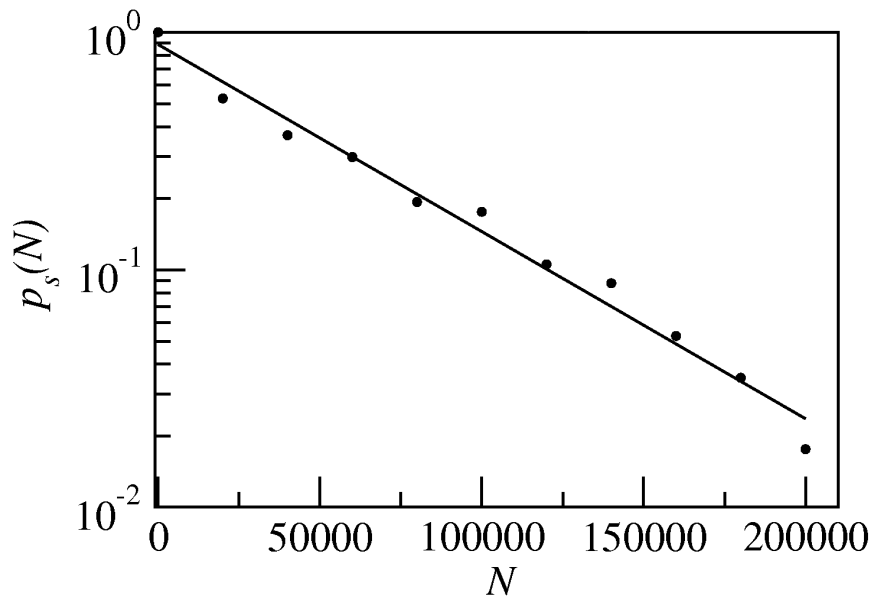
$$\sim 0.6735 n^{3/2} (2.1635)^n$$

Fontana, *BioEssays* 24, 1164 (2002)

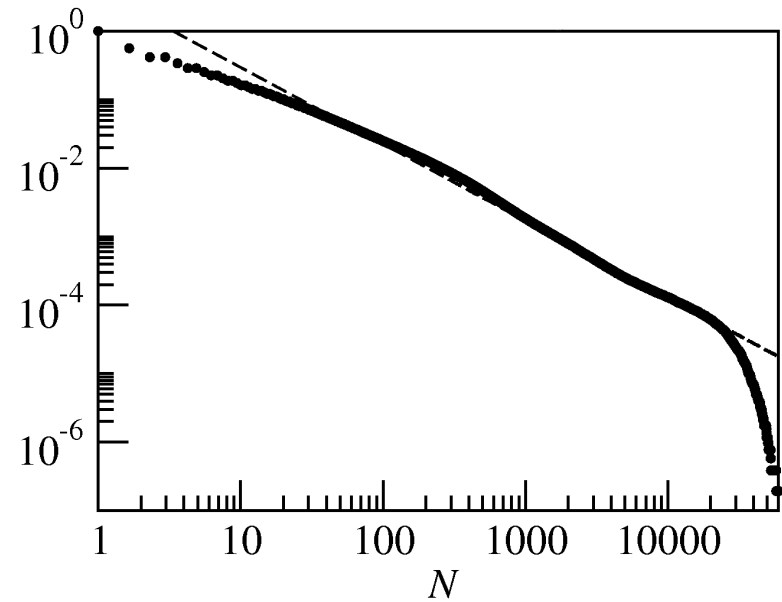
1 10 20 30 40 50 60 70 80 86
 ACAGCAGCACACUAGCAGUCAGUGUCAGACUGGCUAACUGCUGCGUUGCAGUCAGUGCUGCACACUACGCUGUAGUCAUGUGCAG
 ... ((((((... ((((((... ((((((... ((((((...)))))))))...)))))))))...)))))))))...

RNA secondary structure

network-size distribution



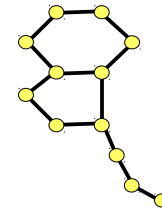
$L = 12$



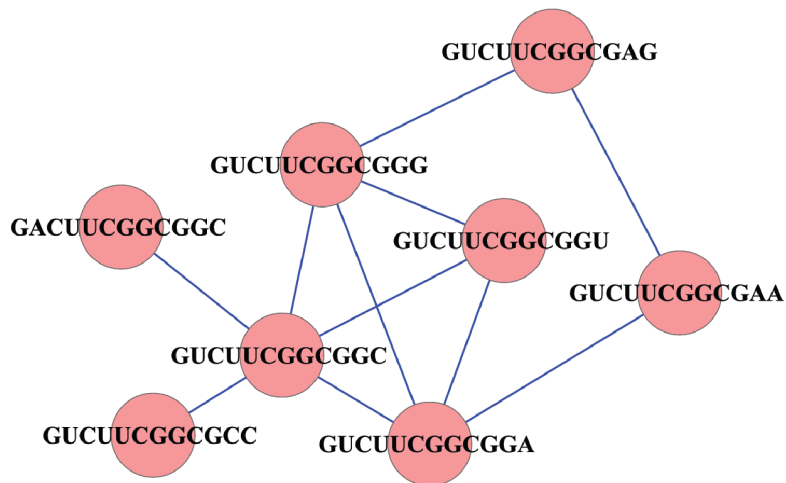
$L = 35$

RNA secondary structure

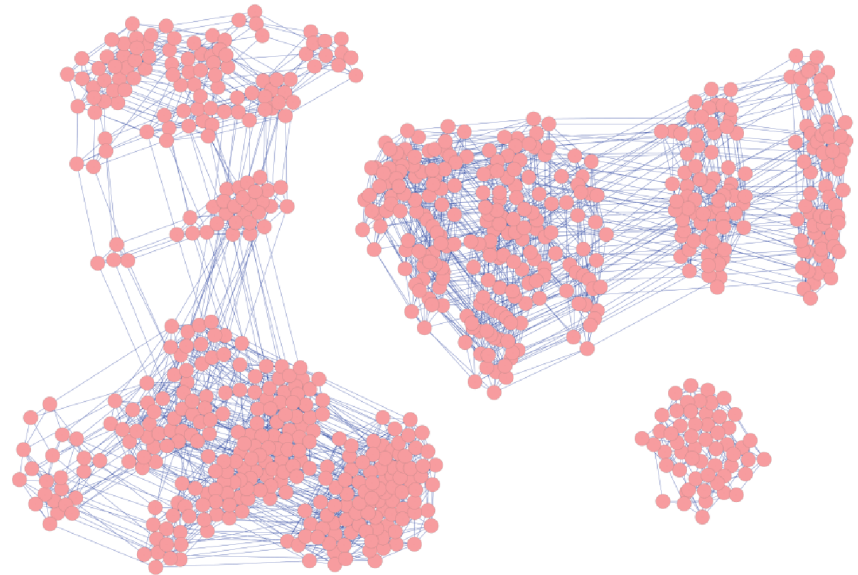
networks topology ($L = 12$)



A

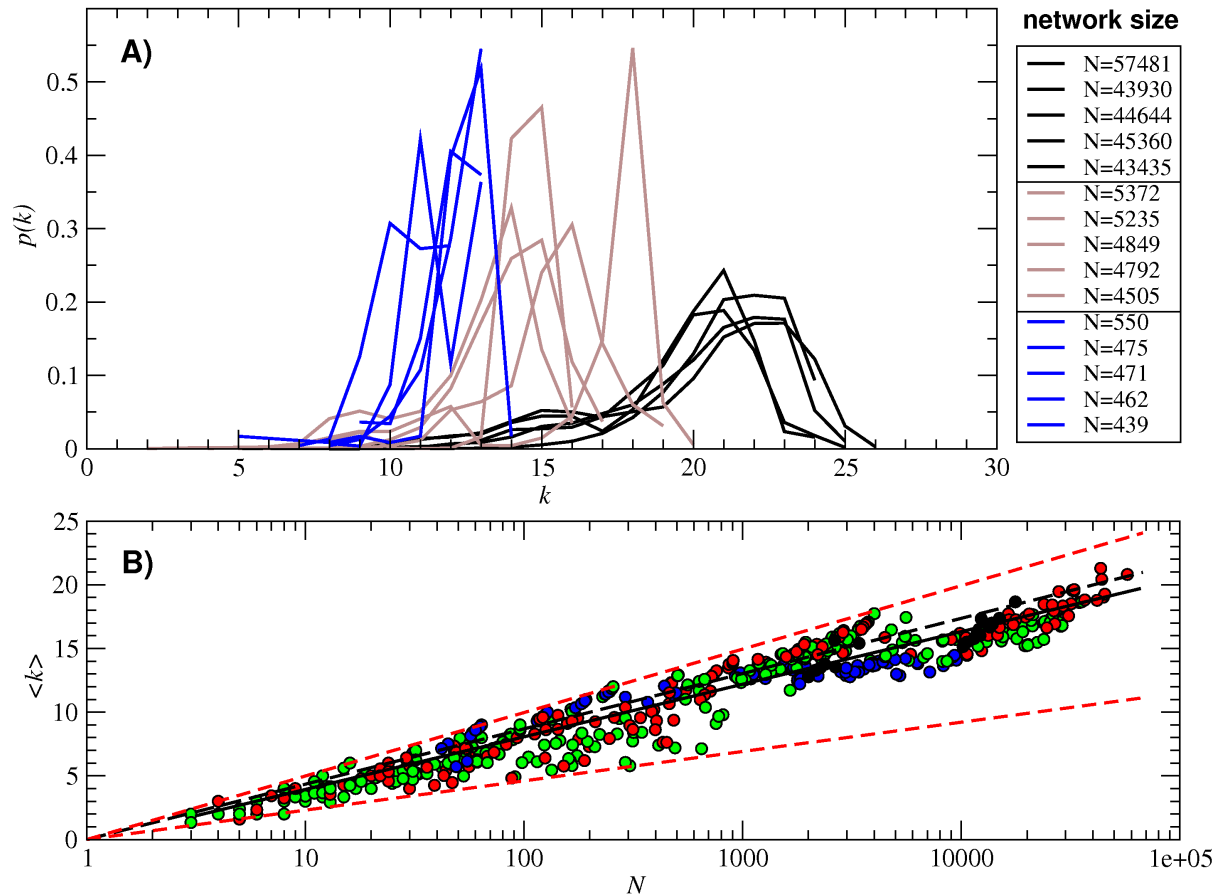


B



RNA secondary structure

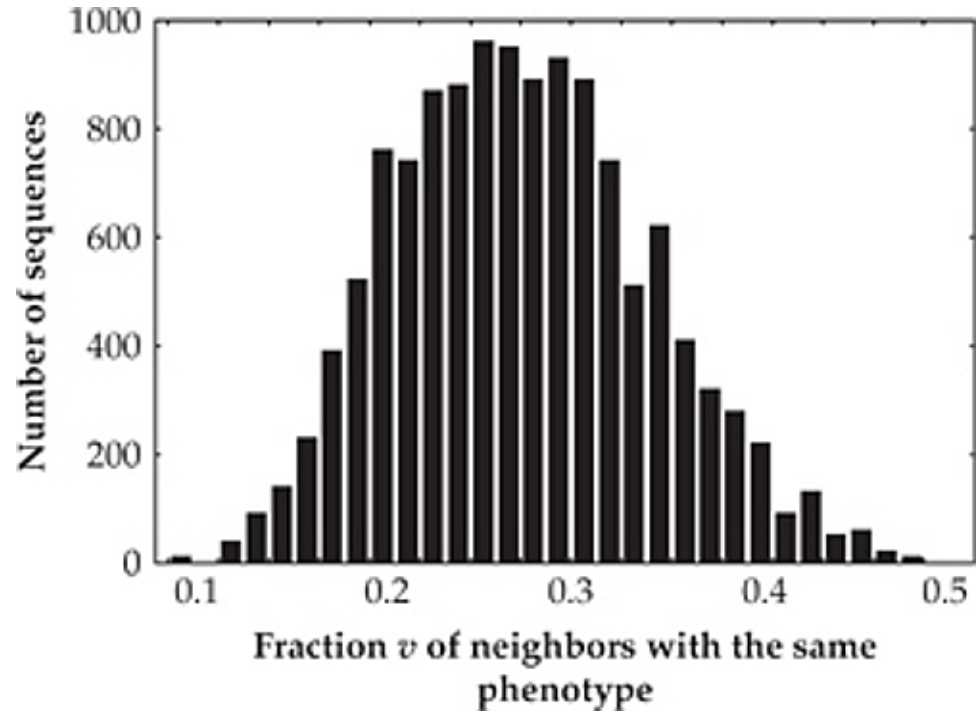
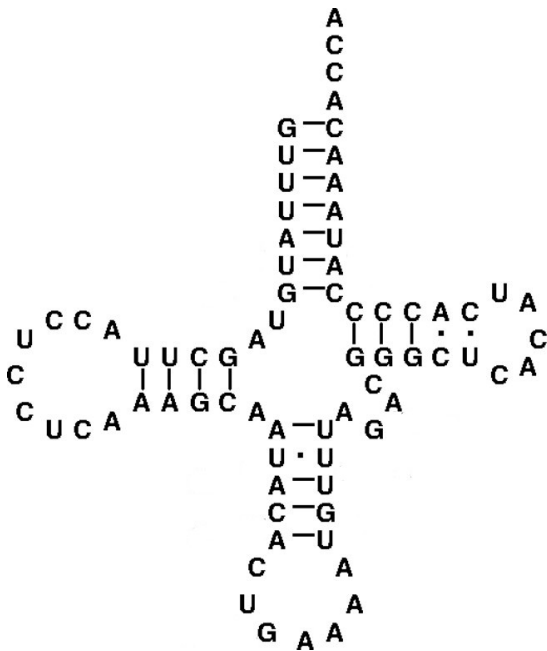
networks topology ($L = 12$)



RNA secondary structure

degree distribution

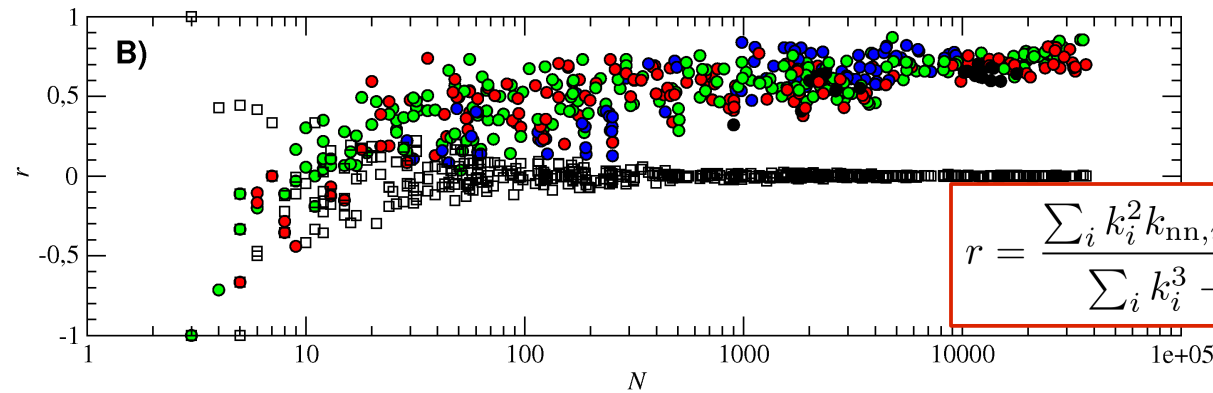
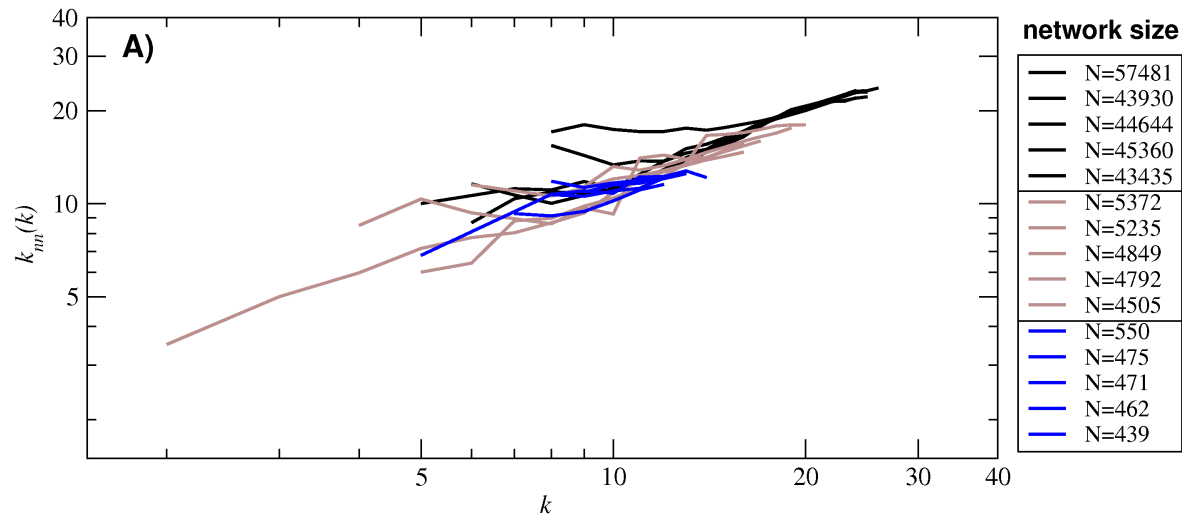
tRNA^{Phe}
($L=76$)



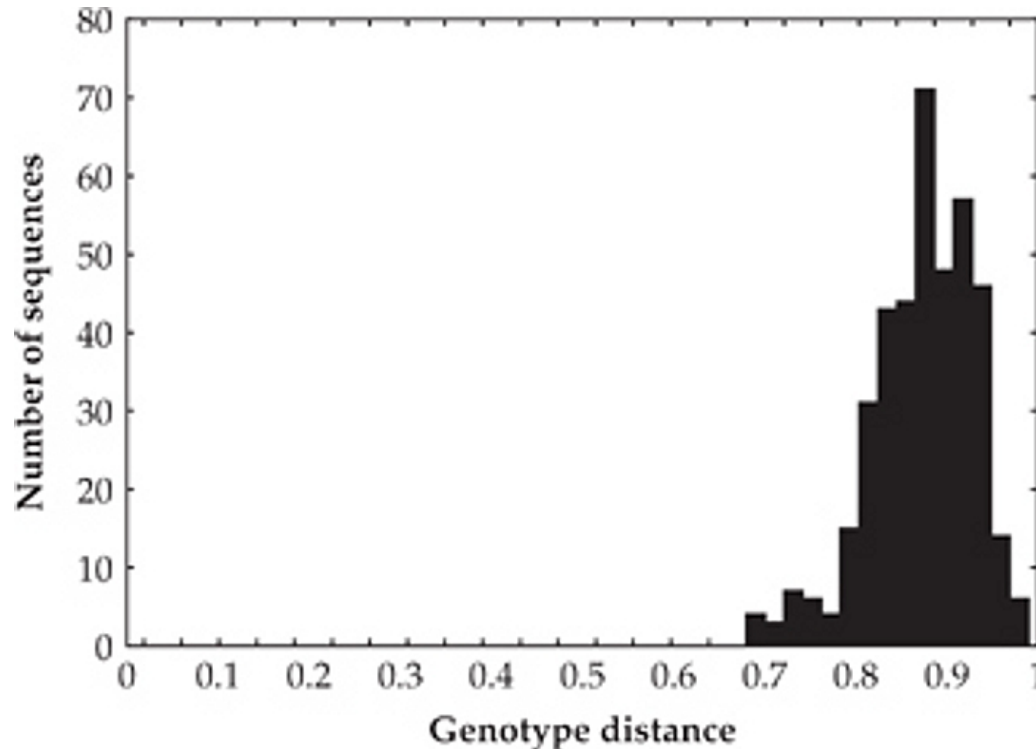
(degree distribution of the genotype network)

RNA secondary structure

networks topology ($L = 12$)

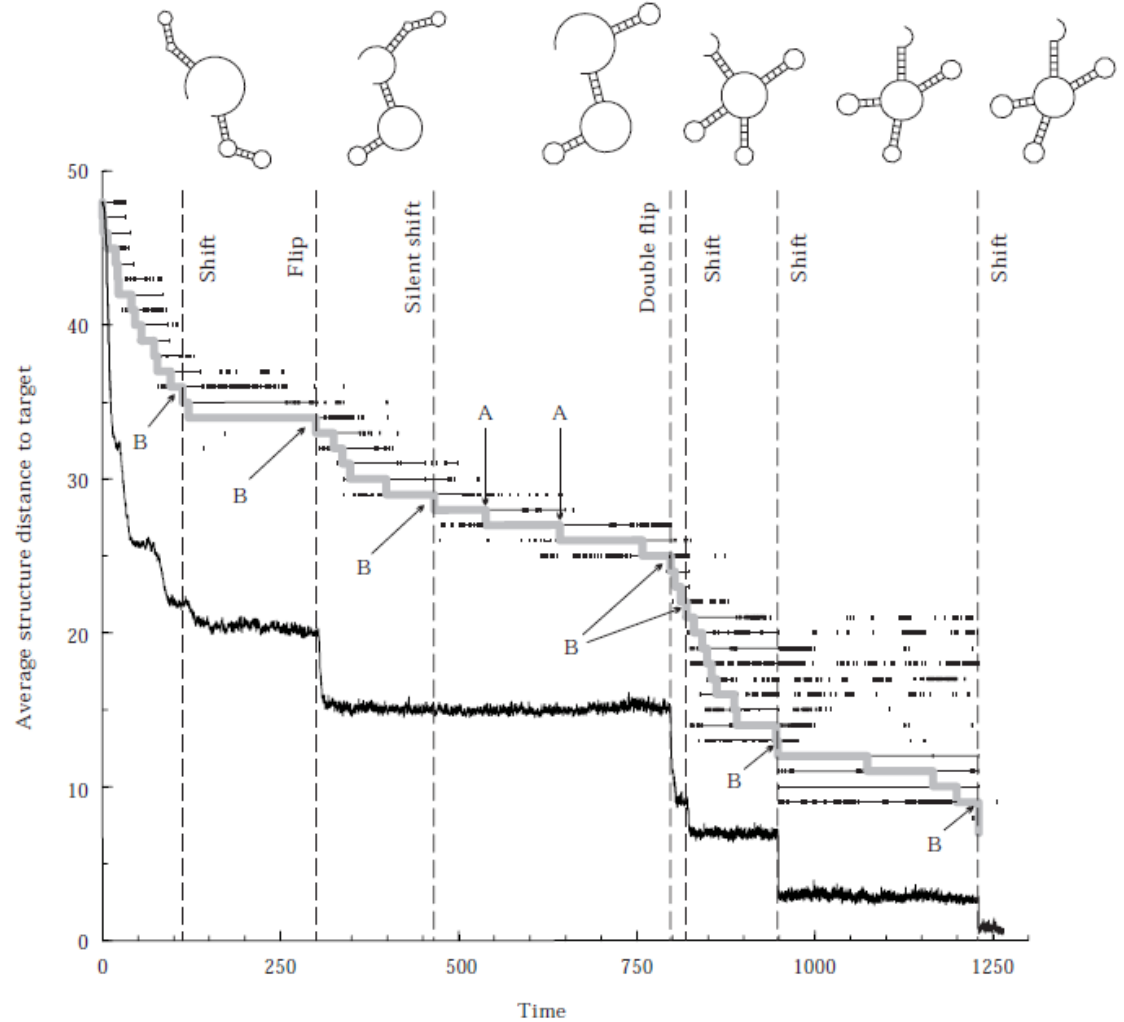
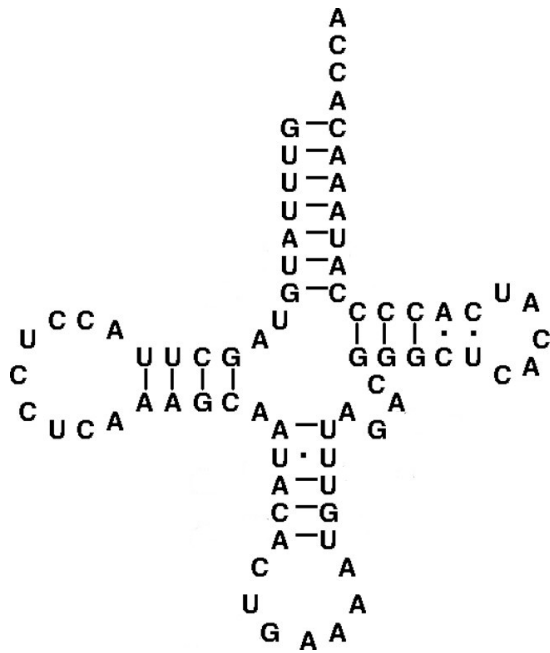


genomic variability

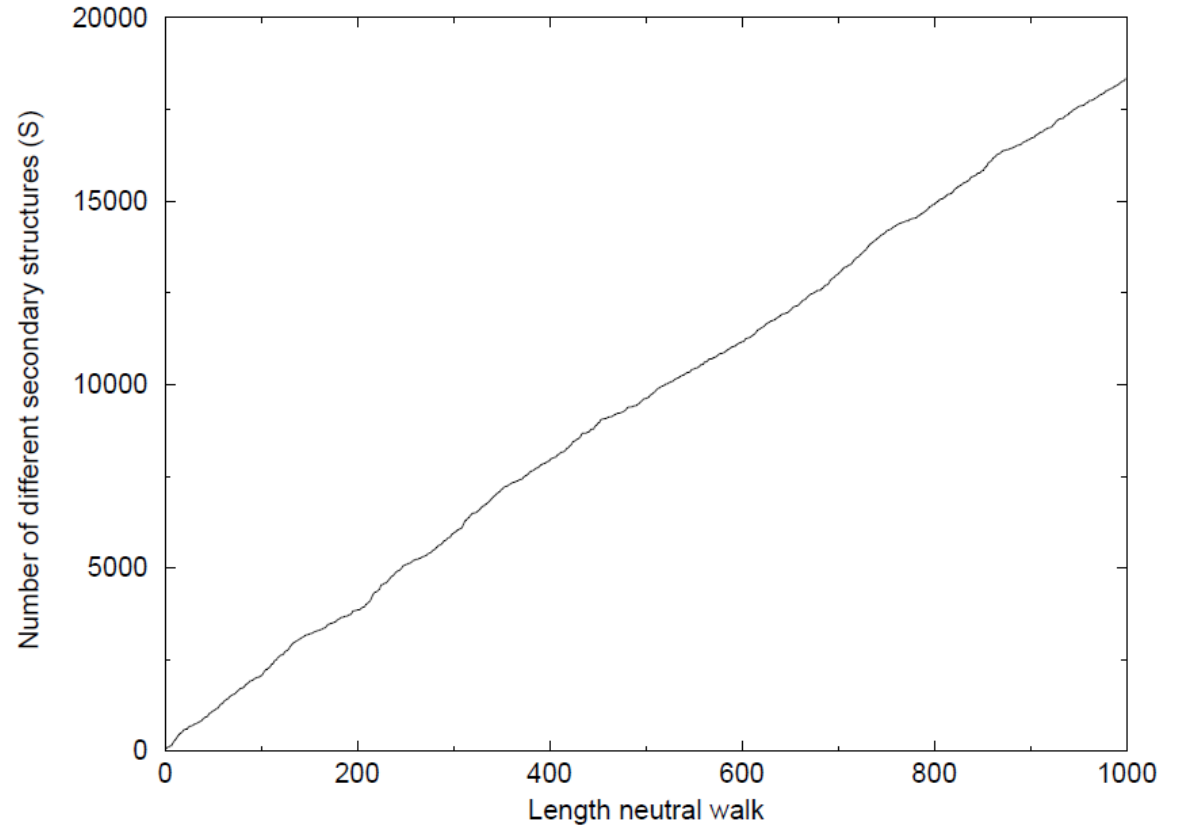
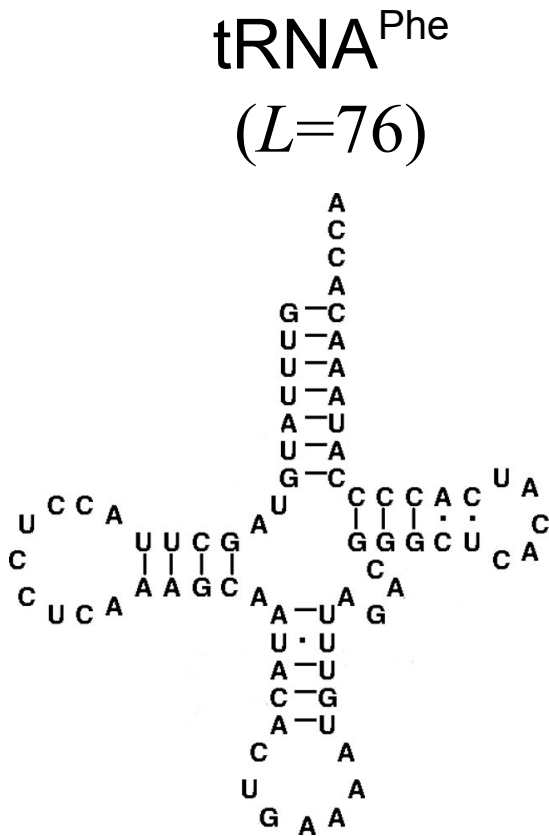


Distance between pairs of genotypes of the same “typical” RNA neutral network, 5000 mutations away of each other ($L=100$; aver. over 466 pairs)

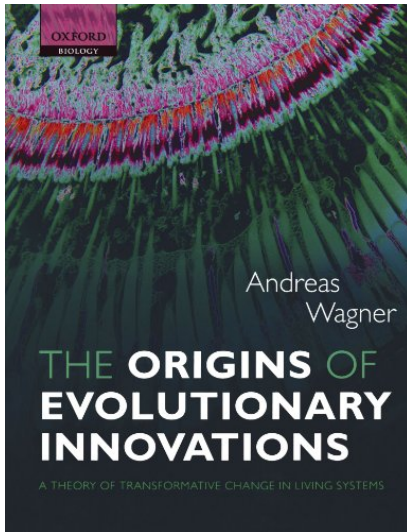
punctuated evolution



closeness of phenotypes

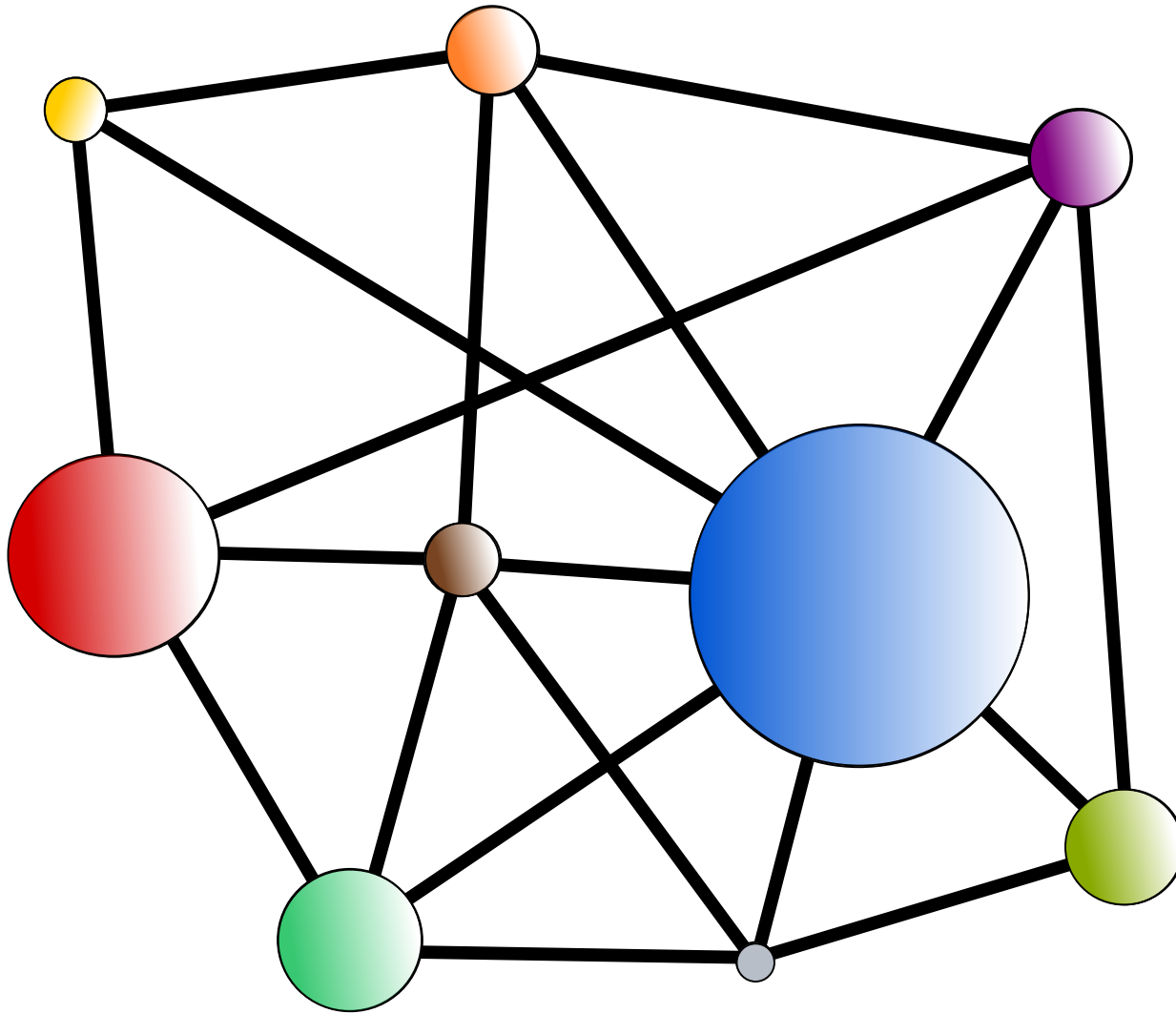


genotype networks



- Huge (but tiny compared to genotype space)
- Percolate genotype space
- Broad (possibly scale-free) size distribution
- Heterogeneous in degree
- Assortative
- Highly interwoven (each phenotype is neighbor of virtually any other one)

phenotype landscape

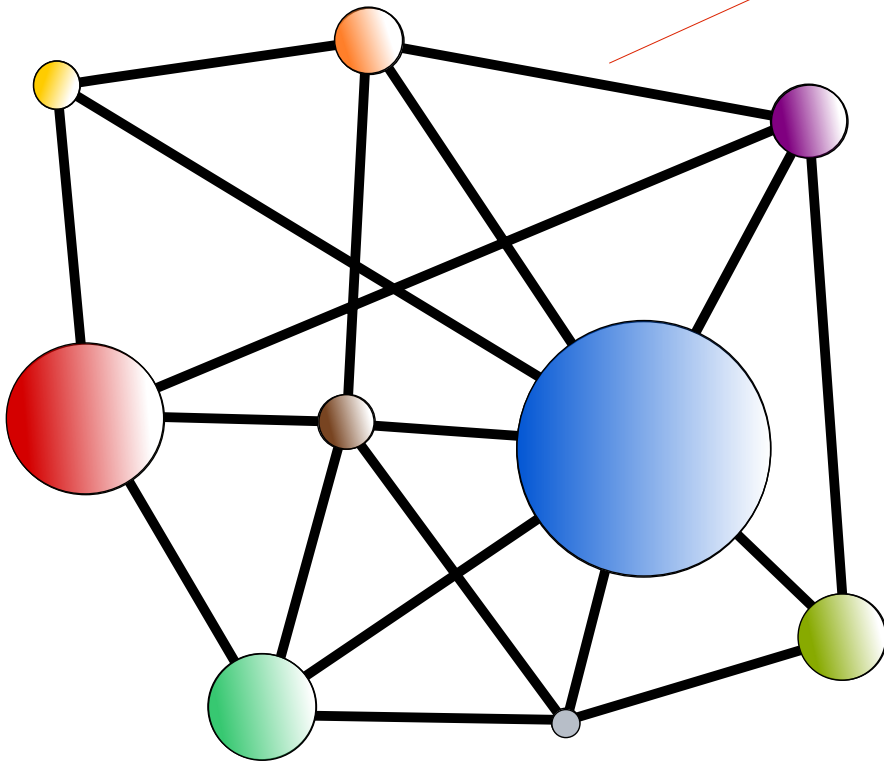


phenotypic mutations

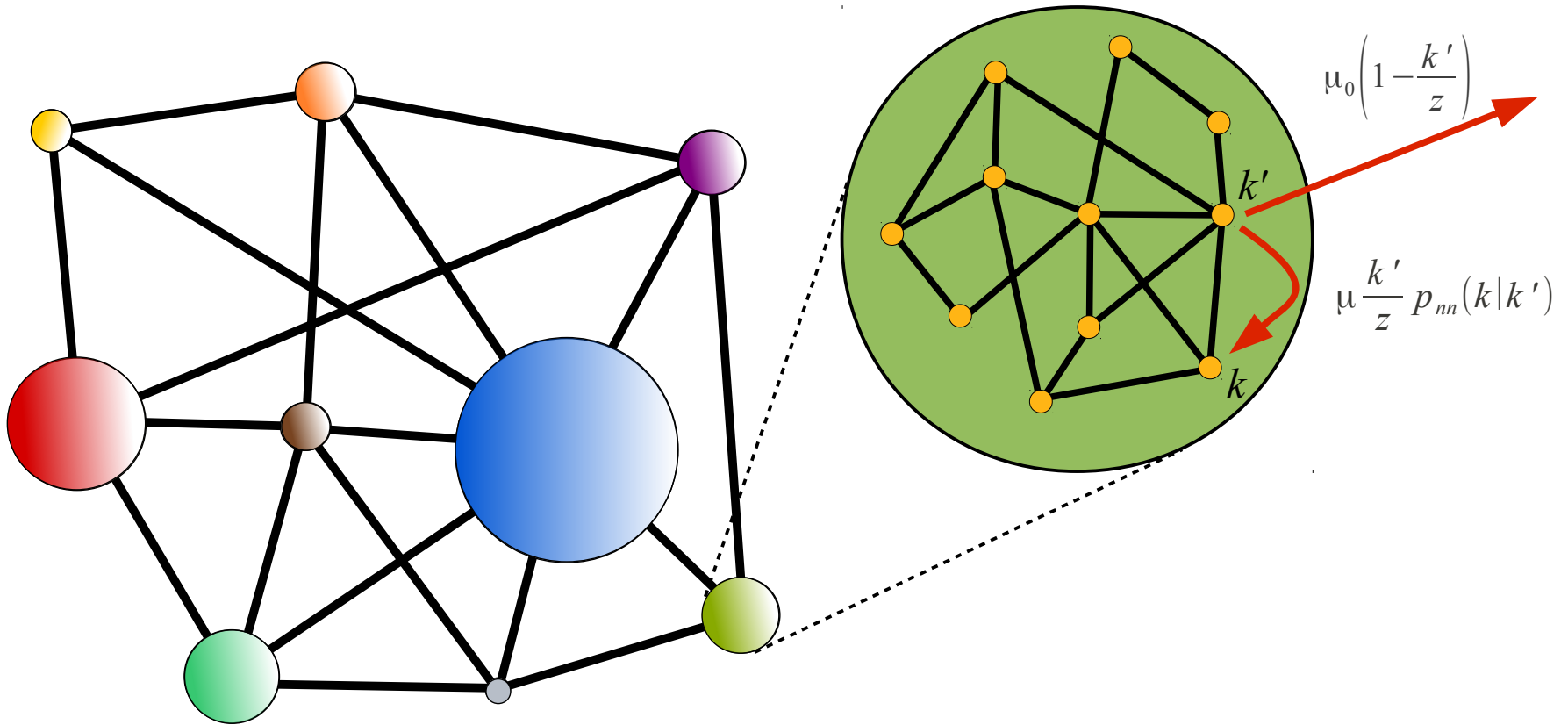
$$w_{ij} = f(d) \Omega(N_i) \Omega(N_j)$$

$$f(d) \sim d^{-\alpha} \quad \alpha \approx 1$$

Manrubia & Sanjuan, Adv. Compl. Sys. **6**, 1250052 (2013)

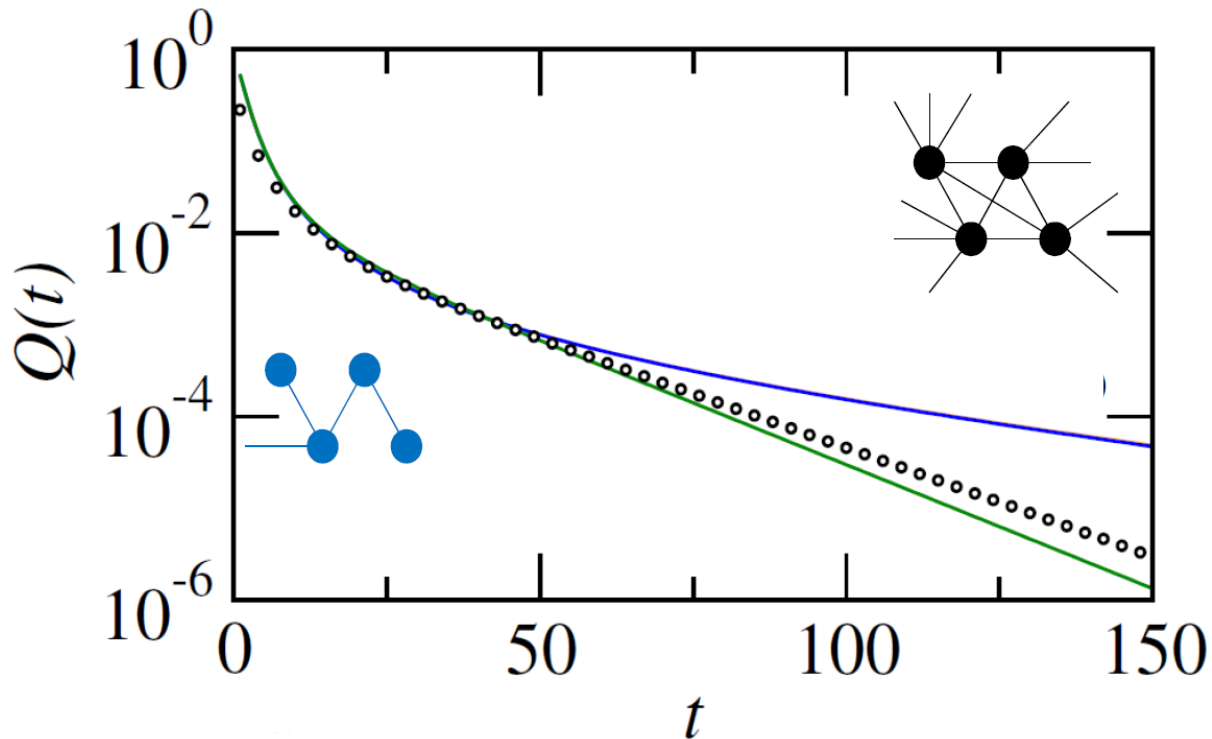


intra-node dynamics



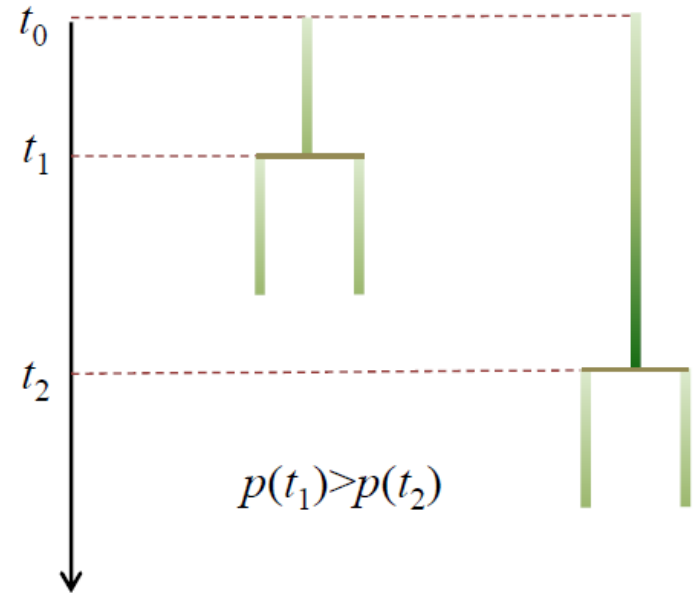
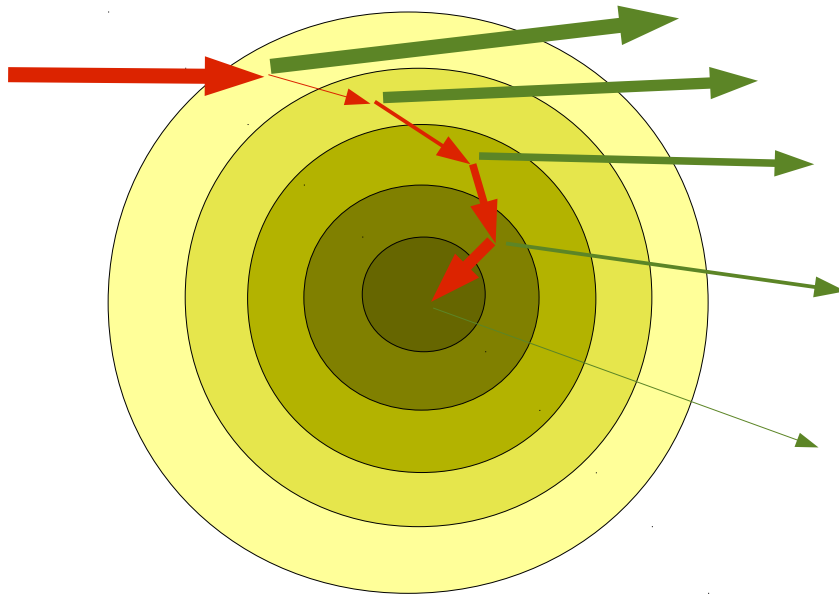
intra-node life-time distribution

$$Q(t) = \sum_{k=0}^z c_k e^{-\alpha_k t} = e^{-\mu_{\text{eff}}(t)t} \quad 0 < \alpha_z < \alpha_{z-1} < \dots < \alpha_1 < \alpha_0 = \mu$$



($\mu_0 = \mu$, all phenotypes equally fit)

phenotypic entrapment

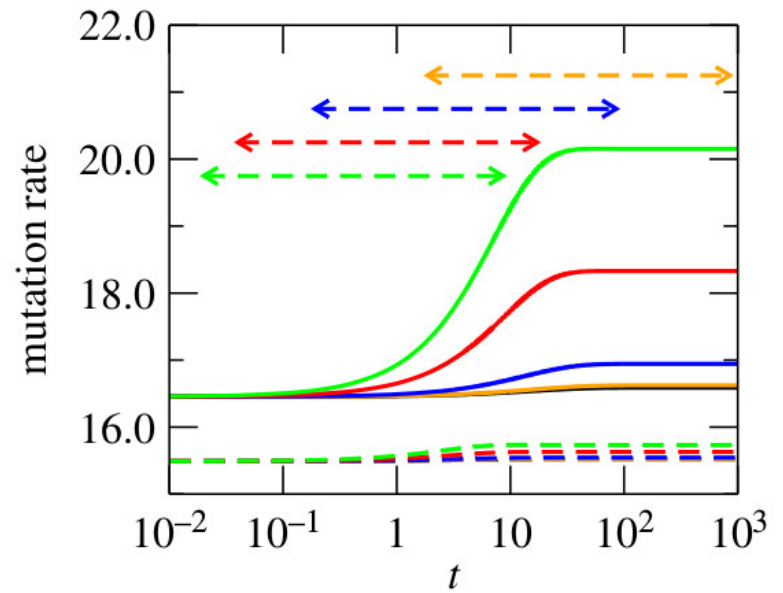
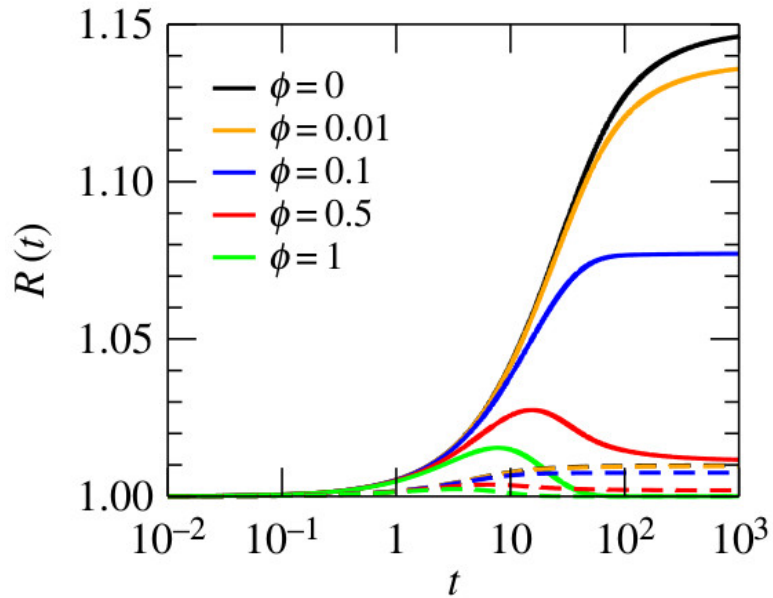


branching probability decreases with branch length

evolution in a phenotype landscape is not markovian!

molecular clock accelerates

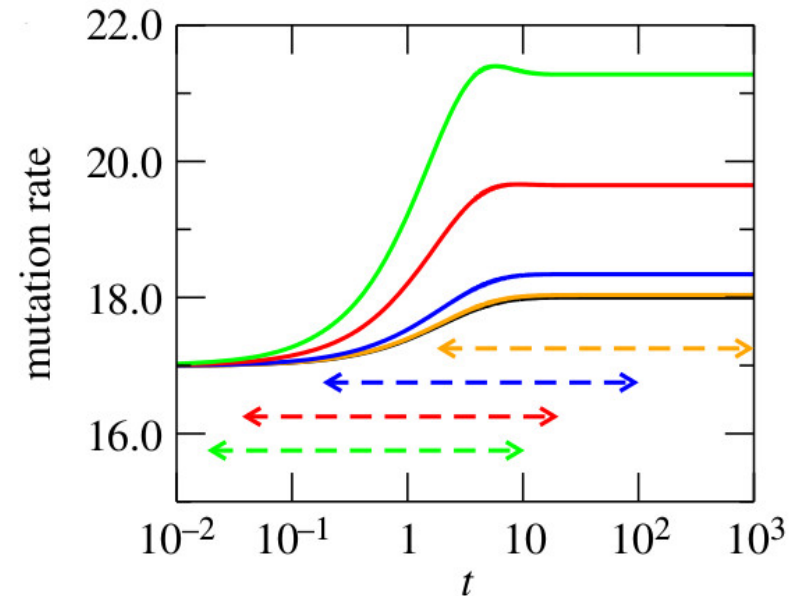
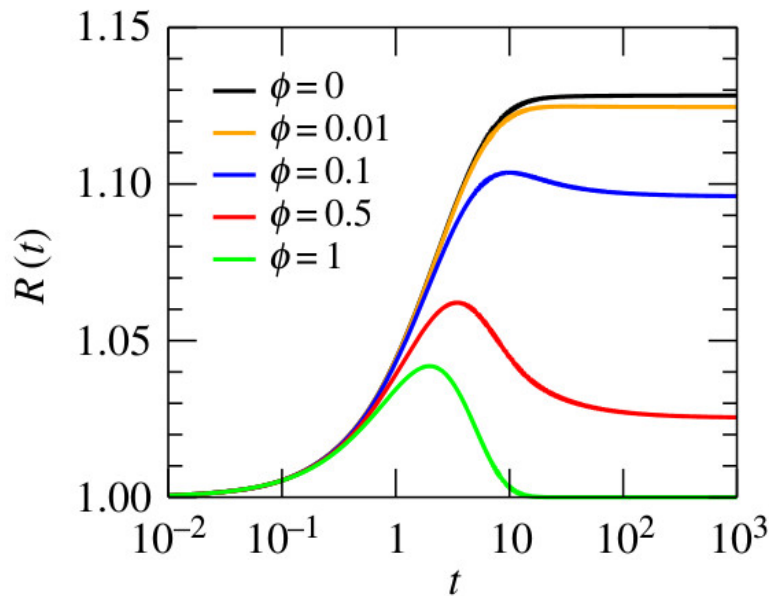
RNA ($L = 12$)



$$\phi \equiv \frac{\text{mean fitness of neighbour phenotypes}}{\text{fitness of focal phenotype}}$$

molecular clock accelerates

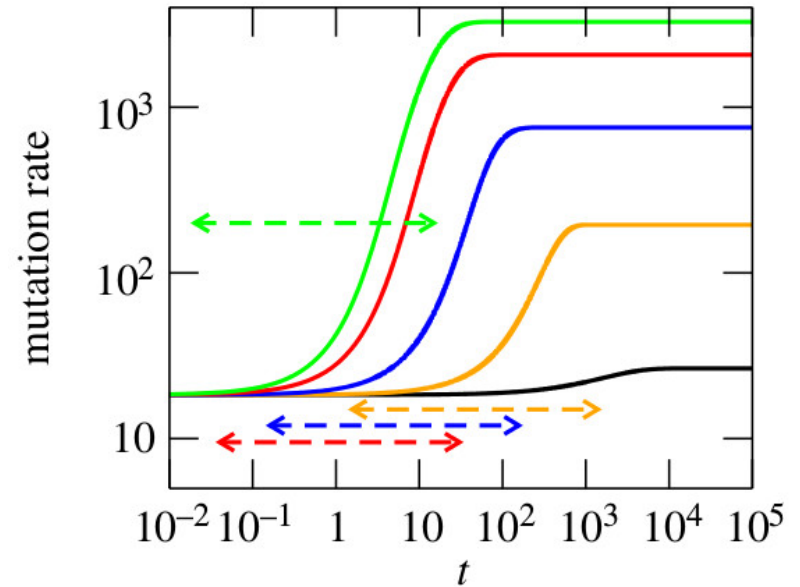
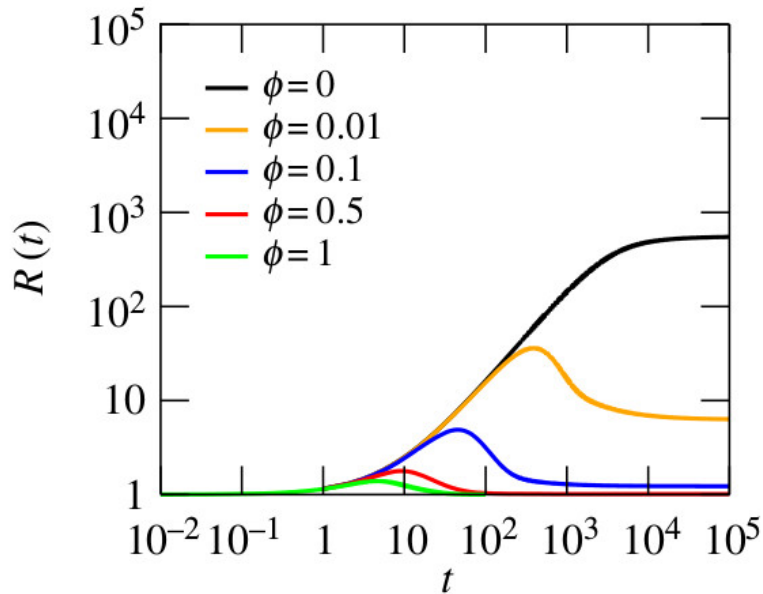
random (Erdős-Renyi)



$$\phi \equiv \frac{\text{mean fitness of neighbour phenotypes}}{\text{fitness of focal phenotype}}$$

molecular clock accelerates

uniform degree distribution, high assortativity ($r \approx 0.9997$)



$$\phi \equiv \frac{\text{mean fitness of neighbour phenotypes}}{\text{fitness of focal phenotype}}$$

Conclusions

- Molecular clock relies on neutral mutation being a **Poisson process**
- Neutral mutations are described through **neutral networks** (high redundancy of the **genotype-phenotype map**)
- Network **heterogeneity** and **assortativity** cause mutational dynamics to deviate from Poisson process
- There is always **overdispersion** and **acceleration** of the molecular clock
- Long branches in phylogenetic trees **tend to be longer**

Take-home message

Beware of the molecular clock!